# Space-like Penguin effects in $B_c$ decays<sup>\*</sup>

Dong-Sheng Du<sup>1,2</sup>, Zheng-Tao Wei<sup>2</sup>

<sup>1</sup> CCAST (World Laboratory), P.O. Box 8730, Beijing 100080, P.R. China

<sup>2</sup> Institute of High Energy Physics, Chinese Academy of Sciences, P.O. Box 918(4), Beijing, 100039, P.R. China<sup>a</sup> (e-mail: duds@bepc3.ihep.ac.cn; weizt@hptc5.ihep.ac.cn)

Received: 15 December 1997 / Published online: 23 June 1998

**Abstract.** The space-like penguin contributions to branching ratios and CP asymmetries in charmless decays of  $B_c$  to two pseudoscalar mesons are studied using the next-to-leading order low energy effective Hamiltonian and factorization approximation. Both the gluonic penguin and the electroweak penguin diagrams are considered. In addition the annihilation diagram contributions are also taken in account. We find that the space-like penguin effects are significant.

# 1 Introduction

The weak decays of B mesons offer a direct way to determine the Cabibbo-Kobayashi-Maskawa (CKM) matrix elements and to explore the origin of CP violation. Penguin diagrams can play an important role in charmless Bdecays. In most cases, attentions were paid to time-like penguin diagram in the literature, and the space-like penguin diagram is considered negligible because of the form factor suppression. In [1], space-like penguin diagram contribution to the branching ratios and CP violating asymmetries in  $B_u^-$ ,  $B^0$ ,  $B_s^0$  decays are considered. The result shows that the space-like penguin amplitude can be enhanced by the hadronic matrix element involving (V-A) (V+A) or (S-P) (S+P) currents, and the space-like penguin effects are large in most charmless B decays.

 $B_c$  meson is considered as the next and the last member of B mesons. Its physics has got intensive attention recently [2, 3].  $B_c$  decay has its own characteristics. The obvious one is that  $B_c$  carries c and b quarks, which are both heavy. So,  $B_c$  decays can be interesting candidates for testing the spectator ansatz. We assume that spectator approximation can be applied in  $B_c$  decays. In our paper, we will consider only b quark decays and take c quark as a spectator. From [3], the future accelerator, Large Hardron Collider (LHC), will produce  $2.1 \times 10^8 B_c$  per year, and can be a good place to study  $B_c$  decays.

In this paper, we study space-like penguin diagram effects in  $B_c$  decays to two pseudoscalars, and we concentrate on the charmless  $B_c$  decays, because penguin diagram plays an important role in these decays. We use the next-to-leading order low energy effective Hamiltonian and factorization approximation to calculate the branching ratios and CP violating asymmetries. In  $B_c$  charmless decays, the annihilation diagram has the same order amplitude as the tree diagram. So the annihilation diagrams should be also taken into account. The result shows that the space-like penguin diagram contributions in  $B_c$  charmless decays are large and cannot be neglected.

## 2 Effective Hamiltonian and factorization approximation

We assume spectator approximation in  $B_c$  decays: the c quark is a spectator and the b quark decays to other light quarks. According to [4], the next-to-leading order low energy effective Hamiltonian describing  $|\Delta B| = 1$  transitions is given at the renormalization scale  $\mu = O(m_b)$  as

$$\mathcal{H}_{eff}(|\Delta B| = 1) = \frac{G_F}{\sqrt{2}} \left[ \sum_{q=u,c} v_q \left\{ Q_1^q C_1(\mu) + Q_2^q C_2(\mu) + \sum_{k=3}^{10} Q_k C_k(\mu) \right\} \right] + H.C.$$
(1)

The CKM factors  $v_q$  are defined as

$$v_q = \begin{cases} V_{qd}^* V_{qb} & \text{for } b \to d \text{ transitions} \\ \\ V_{qs}^* V_{qb} & \text{for } b \to s \text{ transitions.} \end{cases}$$
(2)

The ten operators  $Q_1^u$ ,  $Q_2^u$ ,  $Q_3$ ,  $\cdots$ ,  $Q_{10}$  are given as the following forms:

$$Q_{1}^{u} = (\bar{q}_{\alpha}u_{\beta})_{V-A} (\bar{u}_{\beta}b_{\alpha})_{V-A} Q_{2}^{u} = (\bar{q}u)_{V-A} (\bar{u}b)_{V-A} Q_{3(5)} = (\bar{q}b)_{V-A} \sum_{q'} (\bar{q}'q')_{V-A(V+A)}$$

 $<sup>^{\</sup>star}\,$  Supported in part by National Natural Science Foundation of China

<sup>&</sup>lt;sup>a</sup> mailing address.

$$Q_{4(6)} = (\bar{q}_{\alpha}b_{\beta})_{V-A} \sum_{q'} (\bar{q}'_{\beta}q'_{\alpha})_{V-A(V+A)}$$

$$Q_{7(9)} = \frac{3}{2}(\bar{q}b)_{V-A} \sum_{q'} e_{q'} (q'q')_{V+A(V-A)}$$

$$Q_{8(10)} = \frac{3}{2} (\bar{q}_{\alpha}b_{\beta})_{V-A} \sum_{q'} e_{q'} (\bar{q}'_{\beta}q'_{\alpha})_{V+A(V-A)}$$
(3)

where  $Q_1^u$  and  $Q_2^u$  are the current-current operators, and the current-current operators  $Q_1^c$  and  $Q_2^c$  can be obtained from  $Q_1^u$  and  $Q_2^u$  through the substitution of  $u \to c$ .  $Q_3$ ,  $\cdots$ ,  $Q_6$  are the QCD penguin operators, whereas  $Q_7, \cdots$ ,  $Q_{10}$  are the electroweak penguin operators. The quark q =d or s for  $b \to d$  or s transitions, respectively; the indices  $\alpha, \beta$  are  $SU(3)_c$  color indices;  $(V \pm A)$  refer to  $\gamma_{\mu} (1 \pm \gamma_5)$ .

It is useful to use the renormalization scheme independent Wilson coefficient functions [5]:

$$\bar{\mathbf{C}}(\mu) = \left[\hat{1} + \frac{\alpha_s(\mu)}{4\pi}\hat{r}_s^T + \frac{\alpha(\mu)}{4\pi}\hat{r}_e^T\right] \cdot \mathbf{C}(\mu) ,\qquad(4)$$

where  $\mathbf{C}(\mu)$ ,  $\mathbf{\bar{C}}(\mu)$  are all column vectors. The matrix elements are:

$$\langle \mathbf{Q}^{T}(\mu) \cdot \mathbf{C}(\mu) \rangle \equiv \langle \mathbf{Q}^{T} \rangle_{0} \cdot \mathbf{C}'(\mu)$$
 (5)

where  $\langle \mathbf{Q} \rangle_0$  denote the tree level matrix elements of these operators, and  $\mathbf{C}'(\mu)$  are defined as

$$C'_{1} = \bar{C}_{1}, \qquad C'_{2} = \bar{C}_{2}, \qquad C'_{3} = \bar{C}_{3} - P_{s}/3, C'_{4} = \bar{C}_{4} + P_{s}, \qquad C'_{5} = \bar{C}_{5} - P_{s}/3, \qquad C'_{6} = \bar{C}_{6} + P_{s}, C'_{7} = \bar{C}_{7} + P_{e}, \qquad C'_{8} = \bar{C}_{8}, C'_{9} = \bar{C}_{9} + P_{e}, \qquad C'_{10} = \bar{C}_{10}, \qquad (6)$$

where  $P_{s,e}$  are given by

$$P_{s} = \frac{\alpha_{s}}{8\pi} \bar{C}_{2}(\mu) \left[ \frac{10}{9} - G(m_{q}, q, \mu) \right] ,$$

$$P_{e} = \frac{\alpha_{em}}{9\pi} \left( 3\bar{C}_{1} + \bar{C}_{2}(\mu) \right) \left[ \frac{10}{9} - G(m_{q}, q, \mu) \right] ,$$

$$G(m, q, \mu) = -4 \int_{0}^{1} dx \ x(1-x) \ln \left[ \frac{m^{2} - x(1-x)q^{2}}{\mu^{2}} \right] , (7)$$

here q = u, c. The numerical values of the renormalization scheme independent Wilson Coefficients  $\bar{C}_i(\mu)$  at  $\mu =$  $O(m_b)$  are [6]

$$\bar{c}_1 = -0.313 , \quad \bar{c}_2 = 1.150 , \quad \bar{c}_3 = 0.017 , 
\bar{c}_4 = -0.037 , \quad \bar{c}_5 = 0.010 , \quad \bar{c}_6 = -0.046 , 
\bar{c}_7 = -0.001 \cdot \alpha_{em} , \quad \bar{c}_8 = 0.049 \cdot \alpha_{em} , 
\bar{c}_9 = -1.321 \cdot \alpha_{em} , \quad \bar{c}_{10} = 0.267 \cdot \alpha_{em} .$$
(8)

In (7),  $q^2$  denotes the momentum transfer squared of the virtual gluons, photons, and  $Z^0$  appearing in the QCD and electroweak penguin diagrams respectively. So, the Wilson coefficients  $C'_1$  depend on  $q^2$ . We adopt a simple kinematic picture [1] for two body decays  $B \to PP'$  as illustrated in Fig. 1.



**Fig. 1.** Penguin diagrams for a  $B_c$  meson decaying into two light pseudoscalar mesons P and P' **a** the time-like penguin diagram; **b** the space-like penguin diagram. The subscripts "v" denote "vacuum". The dark dot stands for the contraction of the W-loop



Fig. 2. The Tree diagram and the Annihilation diagram in  $B_c$ decays.  $\mathbf{a}$  the Tree diagram.  $\mathbf{b}$  the Annihilation diagram

The average value of  $q^2$  can be given by

$$\langle q^2 \rangle = m_b^2 + m_q^2 - 2m_b E_q$$
 (9)

where  $E_q$  is determined from

$$E_q + \sqrt{E_q^2 - m_q^2 + m_{q'}^2} + \sqrt{4\left(E_q^2 - m_q^2\right) + m_{q'}^2} = m_b \quad (10)$$

for the time-like penguin diagram; and

$$E_q + \sqrt{E_q^2 - m_q^2 + m_{q'}^2} + = m_b + m_{q'} \tag{11}$$

for the space-like penguin diagram.

In exclusive nonleptonic decays, the current-current operator matrix element can be calculated by factorization approximation and BSW method [7].

For the tree diagram of Fig 2a which correponds to  $b \to q_1 \bar{q}_2 q$ , the matrix element for four-quark operator is defined as:

$$M_{q_{1}q_{2}q}^{PP'} \equiv \langle PP' | (\bar{q}_{1}q_{2})_{V-A} (\bar{q}b)_{V-A} | B_{c}^{-} \rangle$$

$$= \langle P | (\bar{q}_{1}q_{2})_{V-A} | 0 \rangle \langle P' | (\bar{q}b)_{V-A} | B_{c}^{-} \rangle$$

$$= -if_{P}^{\bar{q}_{1}q_{2}} f_{+}^{B_{c}P'} (M_{P}^{2})$$

$$\left( M_{B_{c}}^{2} - M_{P'}^{2} - \frac{M_{B_{c}} - M_{P'}}{M_{B_{c}} + M_{P'}} M_{P}^{2} \right)$$
(12)

where  $f_{+}^{B_c P'}(m_P^2) = \frac{f_{+}^{B_c P'}(0)}{1-M_P^2/(M_{B_c}^{pole})^2} \cdot f_{+}^{B_c P'}(0)$  can be calculated in BSW model, and  $M_{B_c}^{pole} = 6.30 \,\text{GeV}$ . For the time-like penguin diagram, this factorization method is

applied to calculate the time-like penguin operator matrix element.

For the annihilation diagram of Fig. 2b corresponds to  $b\bar{c} \rightarrow q\bar{c}$ , the matrix element is [8]:

$$S_{qcc}^{PP'} \equiv \langle PP' | (\bar{q}c)_{V-A} (\bar{c}b)_{V-A} | B_c^- \rangle$$

**Table 1.** The Branching Ratios of  $B_c$  decaying to two pseudoscalar

			$\operatorname{Br}$			
Decay Mode	Only Tree	Tree+Anni	Tree+Anni+T-like		Tree+Anni+T-like+S-like	
			QCD	QCD+EW	QCD	QCD+EW
$B_c^- \to \pi^- \bar{D}^0$	$1.12 \times 10^{-5}$	$9.60 \times 10^{-6}$	$8.31 \times 10^{-6}$	$8.29 \times 10^{-6}$	$2.27 \times 10^{-6}$	$2.32 \times 10^{-6}$
$B_c^- \to K^- \bar{D}^0$	$8.63 \times 10^{-7}$	$2.81 \times 10^{-6}$	$1.94 \times 10^{-5}$	$1.99 \times 10^{-5}$	$4.82 \times 10^{-5}$	$4.76 \times 10^{-5}$
$B_c^- \to \pi^0 D^-$	$2.54 \times 10^{-8}$	$1.20 \times 10^{-7}$	$5.21 \times 10^{-7}$	$3.73 \times 10^{-7}$	$2.01 \times 10^{-5}$	$1.91 \times 10^{-5}$
$B_c^- \to \eta D^-$	$1.77 \times 10^{-8}$	$3.00 \times 10^{-9}$	$8.05 \times 10^{-6}$	$7.73 \times 10^{-6}$	$7.09 \times 10^{-6}$	$7.10 \times 10^{-6}$
$B_c^- \to \eta' D^-$	$1.76 \times 10^{-8}$	$9.88 \times 10^{-9}$	$6.45 \times 10^{-5}$	$6.43 \times 10^{-5}$	$6.34 \times 10^{-5}$	$6.34 \times 10^{-5}$
$B_c^- \to \eta D_s^-$	$9.03 \times 10^{-10}$	$1.53 \times 10^{-7}$	$8.62 \times 10^{-6}$	$2.71 \times 10^{-6}$	$9.02 \times 10^{-6}$	$8.87 \times 10^{-6}$
$B_c^- \to \eta' D_s^-$	$4.40 \times 10^{-10}$	$1.26 \times 10^{-7}$	$6.09 \times 10^{-6}$	$9.18 \times 10^{-6}$	$1.18 \times 10^{-5}$	$1.17 \times 10^{-5}$
$B_c^- \to K^0 D_s^-$	0	$3.41 \times 10^{-8}$	$1.29 \times 10^{-6}$	$1.27 \times 10^{-6}$	$1.99 \times 10^{-6}$	$1.96 \times 10^{-5}$
$B_c^- \to \bar{K}^0 D^-$	0	$5.87 \times 10^{-7}$	$1.60 \times 10^{-5}$	$1.58 \times 10^{-5}$	$3.60 \times 10^{-5}$	$3.55 \times 10^{-5}$

$$= \langle PP' | (\bar{q}c)_{V-A} | 0 \rangle \langle 0 | (\bar{c}'b)_{V-A} | B_c^- \rangle$$
  
=  $if_{B_c} f^a_+ (M^2_{B_c})$   
 $\left( M^2_P - M^2_{P'} - \frac{M_P - M_{P'}}{M_P + M_{P'}} M^2_{B_c} \right)$  (13)

The matrix elements are computed at momentum transfer  $q^2 = M_{B_c}^2$ . We take the asymptotic form factor  $f_+^a (M_{B_c}^2) = i16\pi \alpha_s f_{B_c}^2/M_{B_c}^2$  [9]. One point should be noted: for the annihilation diagram,  $C'_1 = \bar{C}_2, C'_2 = \bar{C}_1$ .

In  $B_c$  decays, the annihilation diagram is enhanced by the CKM factor  $v_c$ . For the  $b \to d$  process,  $|\frac{v_c}{v_u}| \approx 3$ ; for  $b \to s$  process,  $|\frac{v_c}{v_u}| \approx 57$ . So, the annihilation diagram should be taken into account in  $B_c$  decays.

For the space-like penguin diagram, just like the annihilation diagram, its factorization method is the same as that of the annihilation diagram.

#### **3** Numerical calculation

The decay width for a  $B_c$  meson at rest decaying into two pseudoscalars is

$$\Gamma(B_c \to PP') = \frac{1}{8\pi} | < PP' | H_{eff} | B_c > |^2 \frac{|\mathbf{p}|}{M_{B_c}^2} \quad (14)$$

where

$$|\mathbf{p}| = \frac{\left[ \left( M_{B_c}^2 - (M_P + M_{P'})^2 \right) \left( M_{B_c}^2 - (M_P - M_{P'})^2 \right) \right]^{\frac{1}{2}}}{2M_{B_c}}$$
(15)

is the momentum of the pseudoscalar meson P or P'. The corresponding branching ratios are given by

$$Br\left(B_c \to PP'\right) = \frac{\Gamma\left(B_c \to PP'\right)}{\Gamma_{tot}^{B_c}} . \tag{16}$$

In our numerical calculation, we take [10]  $\Gamma^{B_c}_{tot} = 1.32 \times 10^{-12}$  GeV.

The  $B_c$  meson decay amplitude can be generally expressed as

$$\left\langle PP' \left| H_{eff} \right| B_c^- \right\rangle = \frac{G_F}{\sqrt{2}} \sum_{q=u,c} v_q F_q \,. \tag{17}$$

where q = u, c, and  $F_q$  including the tree and and annihilation and penguin amplitude. The CP-violating asymmetry can be given by

$$\mathcal{A}_{cp} \equiv \frac{\Gamma\left(B_c^- \to PP'\right) - \Gamma\left(B_c^+ \to \bar{P}\bar{P}'\right)}{\Gamma\left(B_c^- \to PP'\right) + \Gamma\left(B_c^+ \to \bar{P}\bar{P}'\right)} = \frac{2Im\left(v_u v_c^*\right)Im\left(F_c/F_u\right)}{|v_u|^2 + |v_c|^2|F_c/F_u|^2 + 2Re\left(v_u v_c^*\right)Re\left(F_c/F_u\right)} \ . (18)$$

We take the decay  $B_c^- \to \eta D^-$  as an example to illustrate the calculation of branching ratio Br and CP asymmetry  $\mathcal{A}_{cp}$  including space-like penguin diagram.

$$\langle \eta D^{-} | H_{eff} | B_{c}^{-} \rangle$$

$$= \frac{G_{F}}{\sqrt{2}} \sum_{q=u,c} v_{q} \left[ \left( a_{2} \delta_{uq} + a_{3} + a_{4} - a_{6} + a_{8} - a_{9}/2 \right) - a_{10} + \frac{2M_{\eta}^{2}}{(m_{d} + m_{d})(m_{b} - m_{d})} (a_{5} - a_{7}/2) \right] M_{ddd}^{\eta D^{-}}$$

$$+ \left( a_{2} \delta_{cq} + a_{3} + \frac{2M_{B_{c}}^{2}}{(m_{d} - m_{c})(m_{b} + m_{c})} \right) \times (a_{5} + a_{7}) + a_{9} S_{dcc}^{\eta D^{-}} \right] .$$

$$(19)$$

where  $a_k$  is defined as

$$a_{2i-1} \equiv \frac{C'_{2i-1}}{3} + C'_{2i} ,$$
  
$$a_{2i} \equiv C'_{2i-1} + \frac{C'_{2i}}{3} , \ (i = 1, 2, 3, 4, 5)$$

and

$$M_{ddd}^{\eta D^{-}} = i f_{\eta}^{\bar{d}d} f_{+}^{B_{c}^{-}D^{-}} \left( M_{\eta}^{2} \right) \left[ \left( M_{B_{c}}^{2} - M_{D^{-}}^{2} \right) \right]$$

**Table 2.** The CP Asymmetries of  $B_c$  decaying to two pseudoscalar. Where the "Tree" means the tree diagram contribution, "Anni" means the annihilation diagram contribution, "T-like" denotes the time-like penguin contributions, the "S-like" denotes the space-like penguin contributions, "QCD" means QCD penguin contributions, and "EW" means electro-weak penguin contributions

			$\mathcal{A}_{cp}$			
Decay Mode	Tree+Anni	Tree+Anni+T-like		Tree+Anni	Tree+Anni+T-like+S-like	
		QCD	QCD+EW	QCD	QCD+EW	
$B_c^- \to \pi^- \bar{D}^0$	-15.1%	-6.8%	-6.8%	-80.6%	-80.1%	
$B_c^- \to K^- \bar{D}^0$	92.6%	-0.7%	-0.7%	19.7%	19.7%	
$B_c^- \to \pi^0 D^-$	92.7%	27.9%	34.1%	15.1%	15.1%	
$B_c^- \to \eta D^-$	-88.6%	14.8%	15.1%	9.2%	9.3%	
$B_c^- \to \eta' D^-$	-47.7%	12.1%	12.1%	11.6%	11.6%	
$B_c^- \to \eta D_s^-$	-13.4%	-0.7%	-1.7%	-1.4%	-1.4%	
$B_c^- \to \eta' D_s^-$	11.8%	-1.8%	-1.4%	0.3%	0.3%	
$B_c^- \to K^0 D_s^-$	0	20.2%	20.4%	-0.6%	-0.6%	
$B_c^- \to \bar{K}^0 D^-$	0	-1.3%	-1.3%	0.1%	0.1%	

$$-\frac{M_{B_c} - M_{D^-}}{M_{B_c} + M_{D^-}} M_{\eta}^2 \bigg]$$

$$S_{dcc}^{\eta D^-} = \frac{1}{\sqrt{3}} f_{B_c} f_+^a \left( M_{B_c}^2 \right) \bigg[ \left( M_{\eta}^2 - M_{D^-}^2 \right) - \frac{M_{\eta} - M_{D^-}}{M_{\eta} + M_{D^-}} M_{B_c}^2 \bigg]$$
(20)

where  $\frac{1}{\sqrt{3}}$  arises from  $\eta = \frac{\bar{u}u + \bar{d}d - \bar{s}s}{\sqrt{3}}$ . The  $a_2\delta_{cq}$  term in (19) is the annihilation diagram contribution.

The numerical results of the space-like penguin contributions to the branching ratios and CP-violating asymmetries are given in Table 1 and 2. We calculate the branching ratios and CP-violating asymmetries with the tree and annihilation and time-like penguin contributions for comparison. All the parameters such as meson decay constants, form factors and quark masses needed in our calculation are taken as  $f_{\pi\pm} = 0.13 \text{ GeV}$ ,  $f_K = 0.160 \text{ GeV}$  [11],  $f_{\pi^0}^{\bar{u}u} = -f_{\pi^0}^{\bar{d}d} = f_{\pi\pm}/\sqrt{2}$ .  $f_{\eta}^{\bar{u}u} = f_{\eta}^{\bar{d}d} = -f_{\eta}^{\bar{s}s} = 0.077 \text{ GeV}$ ,  $f_{\eta'}^{\bar{u}u} = f_{\eta'}^{\bar{d}d} = f_{\eta'}^{\bar{s}s}/2 = 0.054 \text{ GeV}$  [12],  $f_{B_c} = 0.5 \text{ GeV}$  [3],  $f_{+}^{B_c D^-}(0) = 0.595$ ,  $f_{+}^{B_c D^-}(0) = 0.605$ ,  $m_u = 0.005 \text{ GeV}$ ,  $m_d = 0.001 \text{ GeV}$ ,  $m_s = 0.2 \text{ GeV}$ ,  $m_c = 1.5 \text{ GeV}$ ,  $m_b = 4.5 \text{ GeV}$ ,  $M_{B_c} = 6.27 \text{ GeV}$  and the Wolfenstein parametrized CKM parameters are [13]:  $\lambda = 0.22$ , A = 0.8,  $\eta = 0.34$ ,  $\rho = -0.12$ .

## 4 Conclusion and discussion

From Table 1 and 2 we can see the following features:

- (i) For most of the charmless decays, space-like penguin contributions to branching ratios are large. The corrections to the branching ratio and CP violating asymmetries are more than 100%.
- (ii) For space-like penguin in  $B_c$  decays, the contributions of the electro-weak penguins are negligible.

(iii) The annihilation diagram contribution can not be negligible in  $B_c$  decays.

The reason for the large space-like penguin effects can be explained as follows:

- (i) When calculating the matrix element of (V-A)(V+A) current  $< PP'|(\bar{q}b)_{V-A}(\bar{c}c)_{V+A}|B_c >$ , there will appear a factor  $\frac{2m_{B_c}^2}{(m_q-m_c)(m_b+m_c)}$ , this factor will enhance the space-like penguin effects.
- (ii) The form factor  $f_{+}^{a}(m_{B_{c}}^{2})$  is not a suppression factor as usually considered. In  $B_{c}$  decays,  $f_{+}^{a}(m_{B_{c}}^{2}) = 0.077$ , so combine with  $f_{B_{c}} = 0.5$ , the annihilation or space-like penguin matrix element  $S^{PP'}$  is nearly as that of the tree and time-like penguin matrix element  $M^{PP'}$ .
- (iii) The quark mass is an important and sensitive parameter. In our calculation, we have used the current mass. The values of quark mass will have direct effect on the penguin amplitude. Other effects, such as non-factorization effect, final state interation can provide many uncertainties.

Acknowledgements. This work is supported in part by National Natural Science Foundation of China and the Grant of State Commission of Science and Technology of China.

## References

- D. S. Du, Z. Z. Xing, Phys. Lett. B **349** (1995) 215, D. S. Du, M. Z. Yang, D. Z. Zhang, Phys. Rev. D **53** (1996) 249
- D. S. Du, Z. Wang, Phys. Rev. D **39** (1989) 1342; K. Cheung and T. C. Yuan, Phys. Lett. B **325** (1994) 481
- D. S. Du, X. L. Li, Y. D. Yang, Phys. Lett. B 380 (1996) 193
- A. J. Buras, M. Jamin, M. E. Lautenbacher, P. H. Weisz, Nucl. Phys. B 400 (1993) 37; A. J. Buras, M. Jamin, M. E.

Lautenbacher, Nucl. Phys. B **400** (1993) 75; Nucl. Phys. B **408** (1993) 209

- A. Buras, M. Jamin, M. Lautenbacher, and P. Weisz, Nucl. Phys. B **370** (1992) 69; Nucl. Phys. B **375** (1992) 501
- N. G. Deshpande and X. G. He, Phys. Lett. B **336** (1994) 471; Phys. Rev. Lett. **26** (1995) 74; N. G. Deshpande, X. G. He and J. Trampetic, Phys. Lett. B **345** (1995) 547
- M. Wirbel, B. Stech and M. Bauer, Z. Phys. C 29 (1985) 637; Z. Phys. C 34 (1987) 103
- J. Bernabéu and C. Jarlskog, Z. Phys. C 8, 233 (1981); Z. Z. Xing, Phy. Rev. D 53 (1996) 2847
- G. P. Lepage and S. J. Brodsky, Phys. Lett. B 87 (1979) 359
- 10. M. Beneke, Fermilab-Pub-95/401-T
- 11. Particle Data Group, M. Aguilar-Benitez et al., Phys. Rev. D 50 (1994) 1173
- H. Y. Cheng, B. Tseng, IP-ASTP-03-97, NTU-TH- 97-08, September, 1997
- 13. A. Ali, D. London, Preprint CERN-TH 7248/94